

School of Computer Science & Information Technology, DAVV, Indore

Class Name --- M.Tech CS I

Course Code: CS-5216

Assignment - I

Q1 Suppose we are comparing implementations of insertion sort and merge sort on the same machine. For inputs of size n , insertion sort runs in $8n^2$ steps, while merge sort runs in $64n \lg n$ steps. For which values of n does insertion sort beat merge sort?

Q2 Where in a max-heap might the smallest element reside, assuming that all elements are distinct? Is an array that is in sorted order a min-heap? Is the array with values {23; 17; 14; 6; 13; 10; 1; 5; 7; 12} a max-heap?

Q3 Suppose that all element values are equal. What would be randomized quicksort's running time in this case?

Q4 An array of n elements contains all but one of the integers from 1 to $n+1$. (a) Give the best algorithm you can for determining which number is missing if the array is sorted, and analyze its asymptotic worst-case running time. (b) Give the best algorithm you can for determining which number is missing if the array is not sorted, and analyze its asymptotic worst-case running time.

Q5 Give an efficient algorithm to evaluate a polynomial. Perform mathematical analysis and give the time complexity of the algorithm.

Assignment – II

1. Given two strings $str1$ and $str2$ and operations insert, remove or replace can performed on $str1$. Find minimum number of edits (operations) required to convert 'str1' into 'str2'.
2. Write a program to Partition a set into two subsets such that the difference of subset sums is minimum
3. Find minimum number of coins that make a given value. Given a value V , if we want to make change for V cents, and we have infinite supply of each of $C = \{ C_1, C_2, .. , C_m \}$ valued coins, what is the minimum number of coins to make the change?
4. Given a rod of length n inches and an array of prices that contains prices of all pieces of size smaller than n . Determine the maximum value obtainable by cutting up the rod and selling the pieces. For example, if length of the rod is 8 and the values of different pieces are given as following, then the maximum obtainable value is 22 (by cutting in two pieces of lengths 2 and 6)

Assignment – III

1. Give an algorithm for determining if a graph is two-colorable, i.e. if it is possible to colour every vertex red or blue so that no two vertices of the same colour have an edge between them. Your algorithm should run in time $O(V+E)$, where V is the number of vertices and E is the number of edges in the graph. You should assume that the graph is undirected and that the input is presented in adjacency-list form.
2. Perfect matching of an undirected graph on $2n$ vertices is a matching of size n , namely n edges such that each vertex is part of exactly one edge. Give a polynomial time algorithm that takes a tree on $2n$ vertices as input and finds a perfect matching in the tree, if such a matching exists. HINT: Give a greedy algorithm that tries to match a leaf in each step.
3. Implement a greedy algorithm to compute minimum weight spanning tree of a given undirected graph.